

Fig. 1. A metro tunnel project WBS.

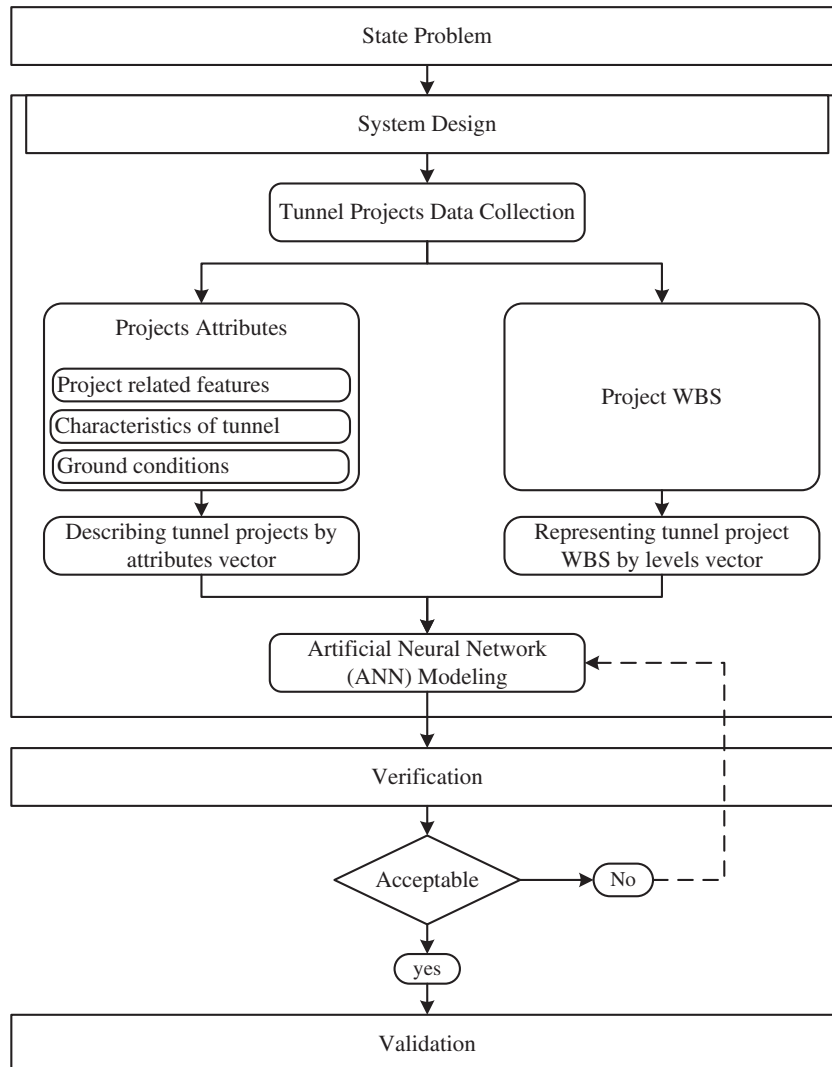


Fig. 2. The overall procedure of proposed methodology.

**Table 1**  
The specification of attributes to describe the projects.

Project attributes	Type of quantity	Bit space	ID
Project related feature			
Client expectations	Lexical	2	A1
Contractor expectations	Lexical	2	A2
Project stakeholders	Lexical	9	A3
Location of the project	Lexical	2	A4
Land possession	Lexical	2	A5
Time	Numerical	8	A6
Cost	Numerical	17	A7
Characteristics of excavation			
Purpose	Lexical	2	A8
Shape	Lexical	3	A9
Diameter	Numerical	11	A10
Length	Numerical	15	A11
Depth	Numerical	10	A12
Construction method	Lexical	5	A13
Ground condition			
Surrounding rock/soil	Lexical	3	A14

#### 4.1. State problem

The main problems of developing WBSs for complex underground projects have been detailed in previous sections. The main purpose of this study is to propose a specific methodology to model the relationship between the attributes of projects and WBSs. This task relies on the premise that the optimal WBS of a complex underground project could be related to the attributes of the project. Previous studies have shown that this relation is very complex and cannot be represented by the classical methods of knowledge representation. However, a substantial number of case histories of previously constructed projects and their WBSs are available. Therefore, artificial neural networks (ANNs) were used to extract the unknown, complex and implicit knowledge of underground projects experts in WBS planning. A brief introduction of this method is provided below.

Artificial neural networks (ANNs) employ a massive interconnection of simple processing elements that are capable of performing a significant number of parallel computations for data processing and knowledge representation [14,15]. ANNs imitate some of the brain's creative processes, albeit in a simplistic way, that cannot be imitated by existing conventional problem-solving methods [16]. The attractiveness of

**Table 2**  
Structure of the proposed neural model with optimum networks parameters.

Networks parameters	WBSL1	WBSL2	WBSL3	WBSL4	WBSL5	WBSL6
No. of input layer neurons	90	195	832	905	678	664
No. of output layer neurons	105	742	815	597	574	882
No. of hidden layer neurons	49	73	57	52	35	62
No. of hidden layer	1	1	1	1	1	1
Training algorithm	BPN	BPN	BPN	BPN	BPN	BPN
Training mode	BT	BT	BT	BT	BT	BT
Stop criteria	CV	CV	CV	CV	CV	CV
Learning rate ( $\eta$ )	0.9	0.9	0.5	0.1	0.5	0.9
Momentum ( $\mu$ )	0.5	0.1	0.5	0.9	0.9	0.5
No. of training epochs	107	109	107	113	113	111
MSE	0.00172	0.00234	0.00095	0.00723	0.00651	0.00096

BPN: Back-propagation.

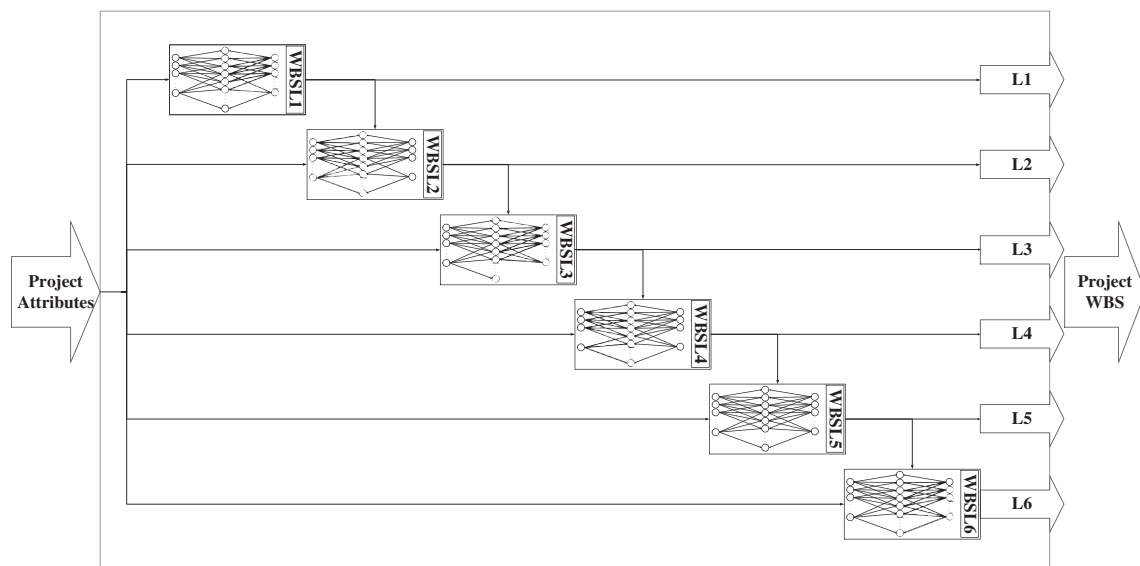
BT: Batch training.

CV: Cross validation.

neural networks comes from their ability to learn and generalize [14]. The artificial intelligence of neural networks is provided by combination of several simple computations at neurons level [17,18]. Each neuron receives inputs, and associated with every input is a weight that corresponds loosely to electrochemical impulses and synaptic connections in the brain [19]. The synaptic weights are determined as the ANN learns. The method used in this study, supervised learning, uses an actual output for each input pattern guiding the learning process. One of the most widely used supervised algorithms is the feed-forward back-propagation network (BPN) [20]. A BPN consists of an input layer, an output layer and one or more hidden layers. In this type of network, the data are fed forward into the network without feedback. The development of ANNs in this study constitutes a cycle of three phases that will be presented in the following sections.

#### 4.2. System design

The main objective of system design is to determine the structure of ANN and learning rules. This phase also involves data collection and partitioning the data into three distinct subsets for use during the training, testing and validation processes. The performance of the neural networks strongly depends on the quality of the training data; thus the



**Fig. 3.** Structure of the proposed neural network model.

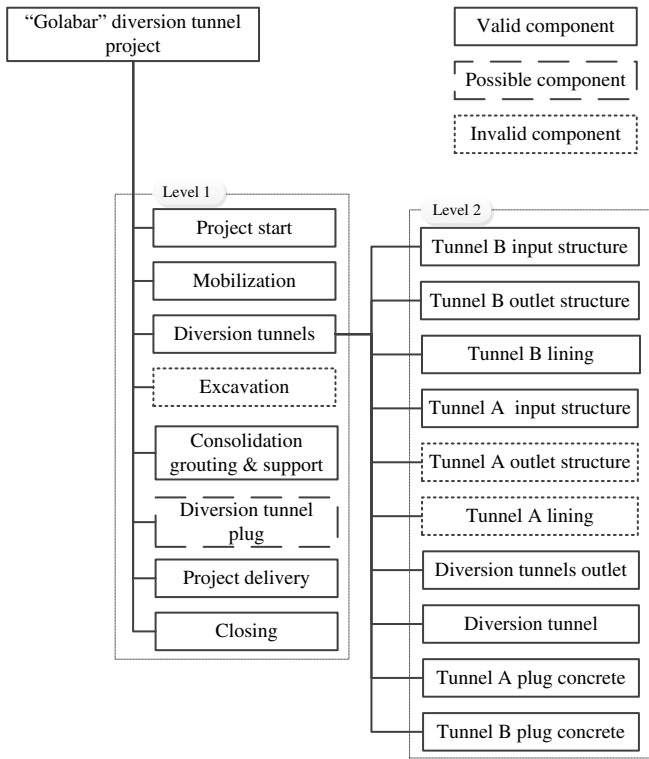


Fig. 4. Developed project WBS for project 1.

sufficient amount of data from previous successful complex underground projects with a quality WBS should be collected to train the neural networks. A dataset of 20 tunnel projects (including 3433 activities) was accumulated. The selected projects are the most successful underground projects constructed in Iran according to tunneling experts, and the project WBSs are high quality. The maximum number of levels in the WBSs of the selected projects is 6. Also the selected WBSs (developed by project contractor) contain 3433 activities in total. The data from 18 projects were used in the verification process, while data from 2 projects were used in the validation process.

The generalization of the ANN models to unseen data will be affected by the size of database. Training data should be sufficiently large to cover the possible variation in the problem domain. Database size can be expanded by obtaining new data. In this study data enrichment was not possible; hence, the leave-one-out method [21] was used for

developing the neural networks. In this method, a network is trained on M-1 (i.e. 18-1) example, and is tested on the one hold-out example. The process is repeated M times. The solution of M network is then averaged to obtain a solution with higher generalizability.

The projects data contain values for project attributes and their work breakdown structures. Project attributes are a limited set of variables that should represent the general nature of a complex underground project. To this end, three major sets of project attributes were defined. The first is the project-related features, which include the total amount of time, total budget and location of the project. The second set is the characteristics of the underground excavation, such as the size and construction method. The third set is ground conditions.

The attributes of project set can be defined by  $A = \{A_i\}$ , ( $0 < i < 14$ ). The members of  $A$  are arranged in a column vector. Then, the values of the project attributes are assigned to the related rows of the resulting vector. Therefore, there are 20 column vectors that will be considered as the inputs for the training, testing and validation patterns. Project attributes are assigned by a combination of lexical and numerical values. As the inputs and outputs of a neural network should be numerical, binary code is assigned to each assignable lexical value. Furthermore, the equivalent binary forms of the project attributes are used for distinct quantities. Table 1 shows the specifications of the complex underground project attributes.

A WBS consists of elements from different levels. Regarding the large number of WBS elements in complex underground projects, the collected WBSs were decomposed into vectors according to the component level to show WBS in the outputs. The vector of the WBS level can be represented by  $L_i = \{w_1, w_2, \dots, w_{n_i}\}$ , where  $L_i$  is the level vector of the WBS at level  $i$ ,  $i$  is the level ID,  $w_i$  is the component and  $n_i$  is the maximum number of components at level  $i$ . Therefore, 20 level vectors with the same size for each level of the WBS are created. These vectors will be considered as the outputs of the training, testing and validating examples.

This study employs feed-forward neural networks with back-propagation learning algorithms, also known as a back-propagation network (BPN). The proposed model is a hierarchical neural network consisting of six different BPNs, which are used to establish the relationships between project attributes and their work breakdown structure. Six BPNs are used due to the hierarchical structure of WBSs. Each BPN has a different configuration, which is used to infer the complex underground project WBS and activities from the project attributes. Fig. 3 shows the structure of the proposed neural model. As shown in Fig. 3, the inputs of WBSL1 only consist of project attributes. This BPN should establish which components should be implemented in the first level of the WBS with respect to the project attributes. Therefore, the output

Table 3  
The project attributes for validation datasets.

Attribute ID	Project 1		Project 2	
	Attribute value	Input neuron value	Attribute value	Input neuron value
A1	High	00	Low	01
A2	High	00	High	00
A3	Members of the parliament Environmental organizations	10000010	Members of the parliament Politicians Owners Nearby residents Public	110111000
A4	Neutral	10	Positive	00
A5	Difficult	0	Difficult	0
A6	42	01010100	11	01000000
A7	18820	001000011001001000	22500	110000010100100000
A8	Diversion tunnel	11	Metro	00
A9	Horseshoe	010	Horseshoe	010
A10	830	01111100110	830	01111100110
A11	870	011001101100000	3070	01111111101000
A12	200	000100110	15	001100000
A13	Drilling & Blasting	0000	NATM	10100
A14	Rock-Moderate	100	Soil-Cohesive	001



of WBSL1 is a row vector whose columns are linked to the individual elements of the first level of the project's WBS. If any columns take a value of 1, the related element can be employed in the first level of the project's WBS. Next, the *L1*-vector and the vector of the complex underground project attributes are considered as the inputs of WBSL2. This network establishes which components should be implemented in the second level with respect to the project attributes and the upper level of the WBS. Therefore, the output of WBSL2 is represented in the second level of the project WBS. Similarly, WBSL3 establishes the third level, WBSL4 establishes the fourth level and so on. As shown in Fig. 3, a six-level complex underground project WBS can be

realized through the learning process. Six networks are used for the identification of the six levels because the maximum level number for the collected WBSs is 6.

### 4.3. Verification

Verification involves training of the proposed neural model using the training and test subsets and simultaneously assessing the network performance by analyzing the mean squared error. The leave-one-out method [21], which is an extreme form of multifold cross-validation, was used to minimize the impact of data dependency on the result.

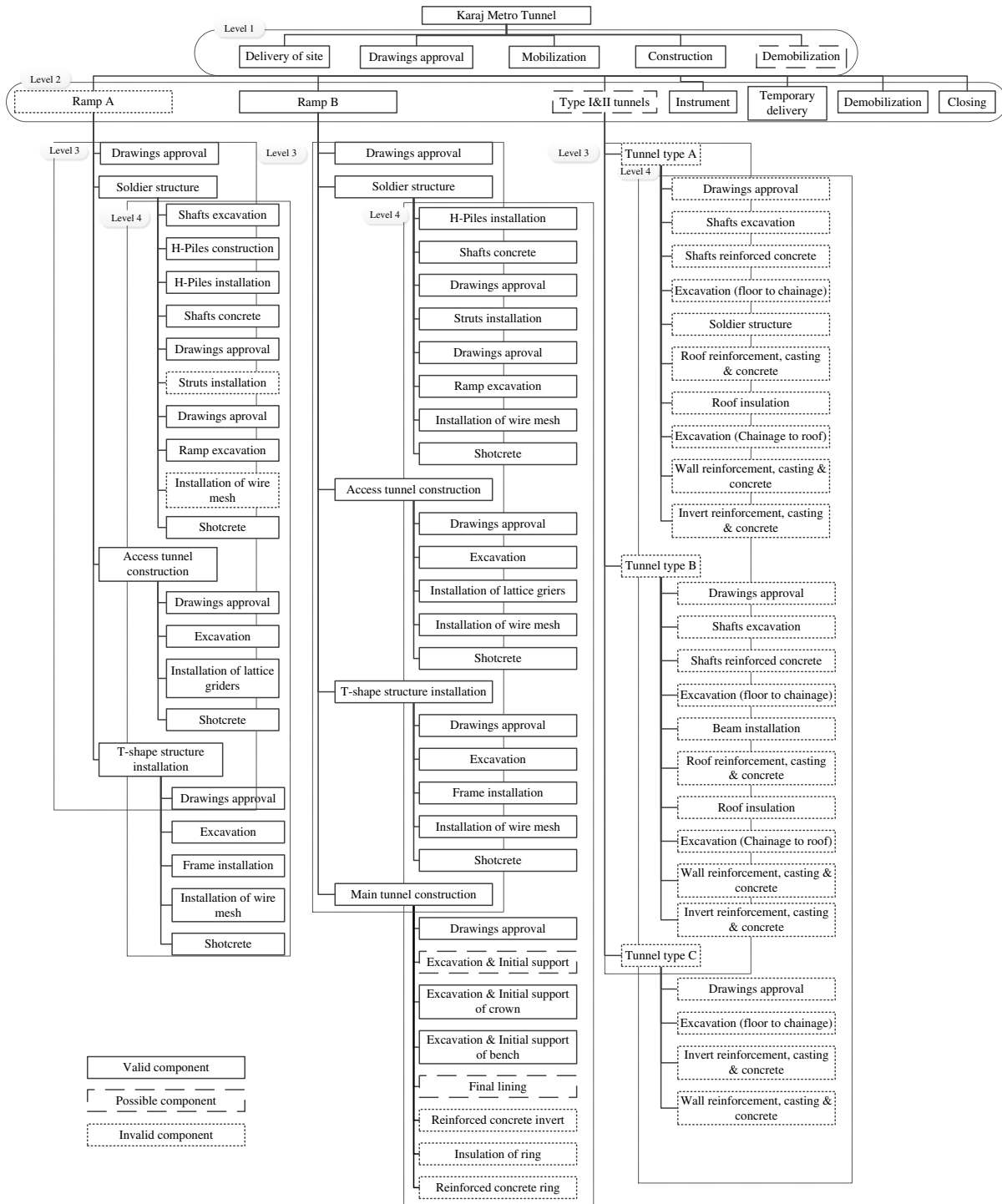


Fig. 5. Developed WBS for project 2 – Levels 1 to 4.

Accordingly, the data from 17 projects (i.e., 18-1) were used to train a model to establish the model parameters, while the hold-out example was used to test the generalization capability of the model. This process was repeated 18 times, with a different example being left out for verification during each run. The squared errors were then averaged over the 18 rounds of training.

BPN training requires the selection of proper values for network parameters. In this study, the optimal values of the network parameters were determined through three stages. In the first stage of simulation, 16 different combinations of learning rate ( $\eta$ ) and momentum ( $\mu$ ) within [0, 1] are investigated. Each combination is trained with the same set of initial weights. At the end of stage 1, the model with the

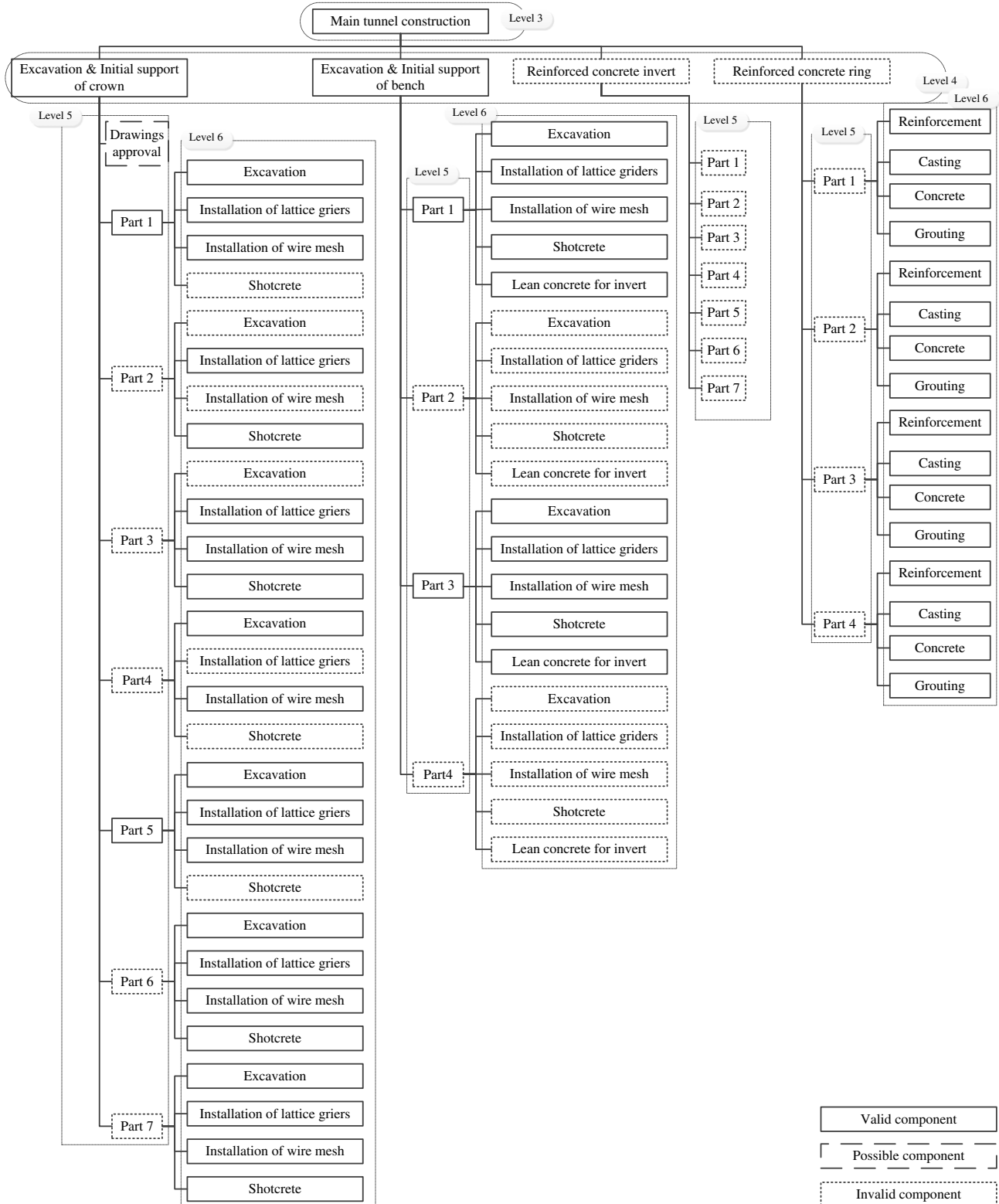


Fig. 6. Developed WBS for project 2 – Levels 5 to 6.





**Table 4**  
Validity of proposed model and its networks.

Network ID	Validation projects	Total number of elements	Number of elements in validity index:			Percentage of elements in validity index:		
			Valid	Possible	Invalid	Valid	Possible	Invalid
WBSL1	Project 1	8	6	1	1	75	12.5	12.5
	Project 2	5	4	1	–	80	20	–
WBSL2	Project 1	10	8	–	2	80	–	20
	Project 2	7	5	–	2	71.43	–	28.57
WBSL3	Project 1	0	–	–	–	–	–	–
	Project 2	12	9	–	3	75	–	25
WBSL4	Project 1	0	–	–	–	–	–	–
	Project 2	71	40	3	28	56.33	4.22	39.44
WBSL5	Project 1	0	–	–	–	–	–	–
	Project 2	28	4	17	7	14.29	60.71	25
WBSL6	Project 1	0	–	–	–	–	–	–
	Project 2	64	47	11	6	73.43	17.19	9.38
Overall model		205	123	33	49	60	16.1	23.9

by a particular index to the total number of elements of the calculated vector ( $n_i$ ) for each project. Then, the average of the three validity percentages within all projects was calculated to obtain the overall validity of each network. Table 4 shows the results of the average validity percentages of the model and its networks.

The validity of the model was estimated with respect to the quantities in Table 4. The valid and possible components of the calculated WBS percentages were found to be 60% and 16.1%, respectively. Therefore, after entering the attributes of a tunneling project, it is expected that 76.1% of the WBS and resultant activities are certainly or possibly valid.

In addition to the relatively accurate recognition of the project WBS elements, several important characteristics of the project WBS were determined by the model. The correct number of WBS levels was identified (for example, two for project 1, and six for project 2). A combination of process-oriented and deliverable-oriented structure was produced for both projects by the model. Project 1, for instance, was decomposed to the processes in level 1, while the second level was a deliverable-oriented decomposition. The level of details for project 1 was two, and levels were decomposed to 8–10 elements. Moreover, the model produced 6 levels for project 2, and several levels were composed of more than 60 elements. Furthermore, in the proposed methodology, different management approaches can be employed to develop the WBS of the project. For instance, the developed WBS by the model for project 2 subdivides the tunnel bench and crown to several parts in level 6, then decomposes the parts into the processes in level 6 such as “Excavation” and “Shotcrete”. Alternatively, another management approach might subdivide the processes to parts in level 6. Therefore, the proposed model was able to recognize the structure of the projects WBSs.

## 6. Conclusions

A new methodology was proposed to plan the WBS of complex underground projects, which assists a planner to make a more informed choice of WBS components and structure regarding project attributes. A hierarchical neural model with 6 BPN networks was developed; each with a different configuration. The outputs of first 5 networks were connected to the inputs of the others, to enable the inference of project structure with respect to the hierarchical structure of the WBS. The proposed methodology focused on two important requirements of generating the WBS of a complex underground project: First, modeling the relationship between the attributes of a project and WBS; and second, to minimize the complexity of the model. This was due to the large number of components of WBS in complex underground projects and various possible structures.

Validation of the results revealed that the proposed neural network model presents a powerful tool for modeling the complex relationship between the attributes of complex underground projects and their work breakdown structures. The approach was demonstrated to be

capable of recognizing the components and structure of the WBS with a sufficient degree of validity that are comparable to those generated by a project planner. Neural networks learn from examples; thus, the performance of the proposed neural model strongly depends on the size and quality of the training data. Due the vast amount of knowledge required for WBS planning in a complex underground project, the proposed model can foster effectiveness in WBS development. In other words, the greater the number of different underground projects that are used to train the networks, the more extensive the data, and the higher the quality of the data used to train the networks, the higher the quality of the resultant overall WBS will be.

Although the neural models herein were developed for the purpose of planning the WBS of a complex underground project during the construction stage, the neural model concept can be extended, particularly to preconstruction stages. The proposed methods for representing the values of project attributes and the WBS can also be modified. Examination of different neural networks structures, other than BPNs, is also a potential topic of future research.

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